

# Application of Wang-Mendel fuzzy algorithm to predict freshwater phytoplankton biomass in East Java, Indonesia

Evellin D. Lusiana, Nanik R. Buwono

Faculty of Fisheries and Marine Science, Brawijaya University, Malang, Indonesia;  
AquaRES Research Group, Brawijaya University, Malang, Indonesia. Corresponding  
author: E. D. Lusiana, evellinlusiana@ub.ac.id

**Abstract.** Phytoplankton are important aquatic biota which act as the primary producer in waters. Nutrient enrichment can lead to excessive abundance of phytoplankton or eutrophication that harms other aquatic organisms. Especially freshwater areas are susceptible to anthropogenic activities that produce organic waste discharges. These activities can worsen the nutrient enrichment in the aquatic ecosystem. This study aimed to predict the freshwater phytoplankton biomass by using the Wang-Mendel fuzzy algorithm as the function of nutrient concentration (nitrate, phosphate) and other water quality parameters (temperature, transparency, pH, dissolved oxygen). The data were collected from various sources that cover 10 rivers/lakes/reservoirs located in East Java province, Indonesia. The results showed that the proposed model performed well in predicting actual phytoplankton biomass. A better model was produced by utilizing all water quality parameters as the predictors instead of the eutrophication model that only accommodated nutrient predictors. Moreover, this model also outperformed the prediction resulting from multiple linear regression.

**Key Words:** eutrophication, fuzzy logic, phytoplankton, prediction model, Wang-Mendel algorithm.

**Introduction.** Plankton are small organisms found in water. They can be divided in two categories, namely zooplankton and phytoplankton (Al-Hashmi et al 2013). Phytoplankton serves as the base of the food chain in aquatic ecosystems. It depends on sunlight for photosynthesis (Inyang & Wang 2020). Therefore, phytoplankton plays a role as natural feed for other aquatic organisms and determines the productivity or trophic status of the waters (Lusiana et al 2019a). It is also a major biological indicator of water quality, as it rapidly reacts to the environmental dynamics (Hallegraeff 2010).

The biomass of phytoplankton needs to be maintained at certain levels (Glibert et al 2010). Low phytoplankton biomass is not proper for aquatic biota growth (Kozak et al 2015), while excessive abundance of phytoplankton (algae bloom, eutrophication) will pollute the water (Sugiura et al 2004). It is harmful to the aquatic ecosystem because it has toxic effects and covers the water area, reducing water transparency (Arend et al 2011). Furthermore, it causes oxygen depletion as the result of the bloom sinking and being decomposed by bacteria (Gobler 2020).

Eutrophication or algae bloom is mainly caused by nutrient enrichment (Lv et al 2011). Nutrients such as nitrates and phosphates are essential for phytoplankton growth (Davidson et al 2014). However, their high concentration in the waters will result in algal bloom that threatens the water system (Wisha et al 2018). Nutrient enrichment is highly associated with organic matter (Barraza-Guardado et al 2013). Escalation of organic matter in waters is usually a consequence of anthropogenic activities which produce waste discharged into waters (Herbeck et al 2013). Specifically, freshwater streams are susceptible to domestic pollution because they are based inland and are directly engaged by human activities (Amoatey & Baawain 2019). Therefore, good water quality management is needed.

The control of phytoplankton biomass as part of water management can be monitored through environmental indicators, especially nutrient concentration (Xu et al 2015). Regression analysis is widely used to predict the abundance of phytoplankton as the function of nutrients (Bode et al 2015; Niu et al 2015; Yuan & Pollard 2018). Nevertheless, it has a low accuracy (Lusiana et al 2019a). The fuzzy method, such as a Wang-Mendel algorithm, can be considered as an alternative to the regression analysis (Alvarez-Estevez & Moret-Bonillo 2018). This algorithm had been implemented to produce better predictions for many problems in finances (Wang 2017) and bioinformatics (Gasparovica et al 2010). The aim of this study was to apply the Wang-Mendel algorithm in predicting freshwater phytoplankton abundance in East Java, Indonesia. This area has many rivers, lakes and reservoirs that suffered pollution because of industrial and domestic activities (Roosmini et al 2018; Musa et al 2019).

## Material and Method

**Description of the study sites and materials.** East Java is the eastern province in Java Island, Indonesia (Figure 1). The water quality data were obtained from 8 freshwater sources in this province. They are Brantas River (Roosmini et al 2018), Bengawan Solo River (Setyaningrum & Agustina 2020), Lake Grati (Mahmudi et al 2019), Lake Pakis (Lusiana et al 2020), Sengguruh Reservoir (Mulyanto 2019), Wlingi Raya Reservoir (Mardiastuti 2019), Sutami Reservoir (Lusiana et al 2019a), Selorejo Reservoir (Manalu 2019), Tanjungan Reservoir (Sari 2020), and Lahor Reservoir (Putra 2017). The datasets were comprised of 7 water quality parameters (temperature, transparency, pH, dissolved oxygen, nitrate, orthophosphate, and phytoplankton biomass) collected from 2016 to 2019. In total, there were 101 samples used in this research. Temperature, transparency, pH and dissolved oxygen were measured *in situ* by a thermometer, Secchi disc, pH meter, and DO meter, respectively, while nitrate and orthophosphate were evaluated *ex situ* in the laboratory of Brawijaya University by using a spectrophotometer (Spectroquant Pharo 300 and GENESYS 10S UV-Vis). The procedures were conducted in accordance to standard methods of APHA (APHA 1989). Water samples were obtained to quantify the phytoplankton at euphotic depth by using plankton nets (pore size 30  $\mu\text{m}$ ). Formalin was used for preservation. Phytoplankton biomass was calculated based on the Lackey drop method (Kadim & Arsad 2016), as follows:

$$D = \frac{C \cdot A_t}{A_s \cdot S \cdot V}$$

Where: D - phytoplankton density ( $\text{cell mL}^{-1}$ ); C - number of organisms counted;  $A_t$  - area of cover slip ( $\text{mm}^2$ );  $A_s$  - area of one strip ( $\text{mm}^2$ ); S - number of strips counted; V - volume of sample under the cover slip (mL).

**Wang-Mendel fuzzy algorithm.** Fuzzy ruled based systems (FRBS) are based on fuzzy logic in soft computing utilized solve real-world problems (Riza et al 2015). It is usually used to tackle problems relating to identification, classification, and regression which contain uncertainty and nonlinearity (Gokulachandran & Mohandas 2012). The basic rule of FRBS is "IF A THEN B", where A and B are fuzzy sets (Tundo & Sela 2018). One of the algorithms that accommodates FRBS is the Wang-Mendel Fuzzy Algorithm. It requires learning and prediction phases in modelling (Figure 2). The learning process in Wang-Mendel Fuzzy Algorithm consists of five steps (Riza et al 2015): 1 - divide input and output spaces into fuzzy sets; 2 - generate the rules of fuzzy from the given datasets; 3 - assign a degree for each generated rule; 4 - produce fuzzy rules combinations; 5 - determine the mapping based on the combination of fuzzy rules. The model resulted from this algorithm is called the Mamdani model (Riza et al 2015) and it can be used to make predictions of desired responses for known predictors.



Figure 1. Research location, East Java, Indonesia.

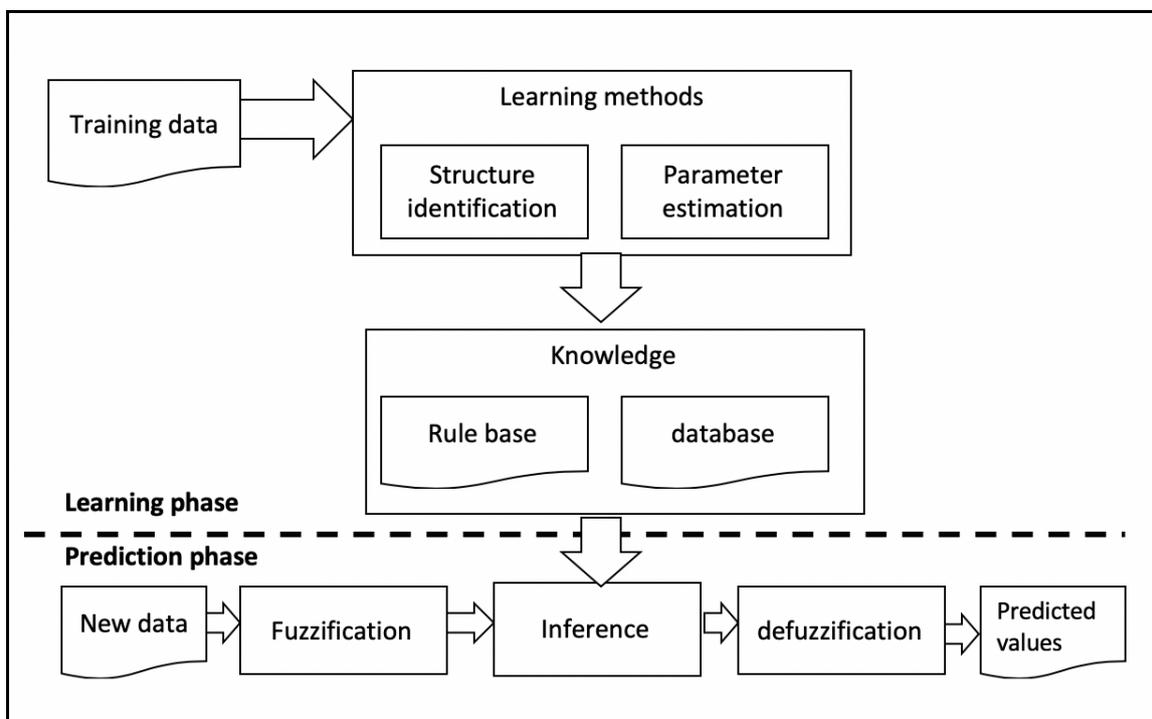


Figure 2. Phase of learning and prediction of a fuzzy ruled based system (Riza et al 2015).

**Data preparation, input selection, and performance evaluation.** 3 types of models using the Wang-Mendel algorithm were employed in estimating phytoplankton biomass: 1 - WM1 or the eutrophication model which used nutrient concentration (nitrate and

orthophosphate) as the predictors; 2 - WM2 model that used all water quality parameters; 3 - WM3 model which included water quality parameters that had significant relationships with phytoplankton biomass. The raw dataset in this study was transformed by natural logarithm transformation to reduce bias due to differences in the magnitude and units (Hazra & Gogtay, 2016) of variables. The data were then analyzed using the Pearson correlation (Schober & Schwarte, 2018) as in the following equation to determine the association of each water quality parameter to phytoplankton biomass.

$$r_{xy} = \frac{n \sum_{i=1}^n X_i Y_i - \sum_{i=1}^n X_i \sum_{i=1}^n Y_i}{\sqrt{\left[ n \sum_{i=1}^n X_i^2 - \left( \sum_{i=1}^n X_i \right)^2 \right] \left[ n \sum_{i=1}^n Y_i^2 - \left( \sum_{i=1}^n Y_i \right)^2 \right]}}$$

Where: X=first variable; Y=second variable; n=sample size

Every significant parameter ( $p < 0.05$ ) was included as a predictor to estimate phytoplankton biomass in the WM3 model. The dataset partitioned into data training (80%) and data testing (20%) (Prashanth et al 2020). In addition, to measure the performance of the Wang-Mendel fuzzy algorithm, a multiple linear regression (MLR) of each model was also run, for comparison. The accuracy of each method was indicated by the high coefficient of correlation (R), lower Mean Absolute Error (MAE), and Root Mean Square Error (RMSE) (Ahmed & Shah 2017).

## Results and discussion

**Water quality parameters.** Table 1 presents basic statistics of data used in this research.

Table 1

Basic statistics of physico-chemical water quality parameters and Pearson correlation results

Variable	Unit	Minimum	Maximum	Mean	SD	CorrPhyto	p
Temperature	°C	25	32	28.82	1.87	-0.118	0.245
Transparency	m	0.06	2.36	0.83	0.58	-0.268	0.007*
pH	-	6.52	8.3	7.51	0.46	-0.341	0.0005*
DO	mg.L <sup>-1</sup>	5.39	13.3	8.87	1.71	0.023	0.823
Nitrate	mg.L <sup>-1</sup>	0.05	2.81	0.88	0.74	-0.155	0.876
Orthophosphate	mg.L <sup>-1</sup>	0.01	0.87	0.24	0.26	0.027	0.793
Phytoplankton biomass	cell mL <sup>-1</sup>	280	25850	4573.75	4875.5	-	-

Note: SD - standard deviation; CorrPhyto - correlation with phytoplankton biomass; DO - dissolved oxygen; \* - significant correlation.

Table 1 shows that the average temperature in the studied sites was 28.82°C. It is optimum for algae growth (Renaud et al 2002). On the other hand, water transparency was 0.83 m, with big deviations. The major threat of water eutrophication is that it can damage the balance of water ecosystems. It can reduce sunlight penetration and decrease the photosynthesis rate of plants in the water (Yang et al 2008). The pH values were 7.51 on average, with small deviations. This is ideal for freshwater algae, because lower pH can cause the deterioration of chloroplasts (Kim et al 1999).

The concentration of dissolved oxygen (DO) was between 5.39 and 13.3 mg L<sup>-1</sup>. DO is heavily influenced by temperature. An increase in temperature will decrease DO and reduce phytoplankton abundance and biodiversity (Takarina & Patria 2017). Nitrate and orthophosphate are two parameters which directly determine the phytoplankton standing stock. The lack of nutrients is a limiting factor in the growth of phytoplankton (Vrede et al 2009). Nutrient enrichment can result in alga blooming and eutrophication

(Lusiana et al 2019b). The phytoplankton biomass in this research revealed high variations from the lowest of 280 cells mL<sup>-1</sup> to 25850 cell mL<sup>-1</sup>. Therefore, it can be classified into oligotrophic to eutrophic categories (Baban 1996). Eutrophication has many bad effects for the ecosystem (Pasztaleniec 2016). Commonly, it contributes to the alteration of phytoplankton community as well as uncontrolled production of toxic species such as *Cyanobacteria* and filamentous green algae (Søndergaard et al 2011).

Based on the correlation analysis, only pH and DO that have significant correlation with phytoplankton biomass ( $p < 0.05$ ). Hence, these parameters were included in the WM3 model in this present study. Finally, the three models used in this study were WM1 (nitrate and orthophosphate predictors), WM2 (all water quality parameters predictors), and WM3 (pH and DO predictors).

**Model prediction results and performance evaluation.** The model of Wang-Mendel (WM) fuzzy algorithm used training, testing, and complete datasets (training+testing) for various predictor combinations. The 3 performance indicators were calculated to evaluate the accuracy of the phytoplankton biomass prediction model. Table 3 shows the MAE, RMSE, and correlation coefficient (R) between observed and predicted values of each proposed model. Generally, the WM model performances were adequate for each model in predicting phytoplankton biomass. The WM1 model or eutrophication model worked well with high correlation coefficient, greater than 0.9 except for the testing dataset ( $R = 0.21$ ), while the RMSE and MAE were 0.322 and 0.445 for training, respectively, and 0.467 and 0.554 for testing, respectively. On the other hand, all correlation coefficients for WM2 model were greater than 0.9, supporting low RMSE and MAE. Meanwhile, the performance of WM3 was poorer than that of other models for all indicators. Therefore, out of the 3 proposed Wang-Mendel fuzzy algorithm models, the model with all water quality parameters as predictors (WM2 model) was the best model because it had the best performance.

Table 2

Performance evaluation of Wang-Mendel (WM) fuzzy algorithm for training, testing, and whole dataset

<i>Model</i>	<i>Dataset</i>	<i>MAE</i>	<i>RMSE</i>	<i>R</i>
WM1	Training	0.322	0.445	0.927
	Testing	0.467	0.554	0.21
	Complete	0.35	0.468	0.916
WM2	Training	0.099	0.135	0.993
	Testing	0.676	0.867	0.993
	Complete	0.21	0.399	0.938
WM3	Training	0.44	0.603	0.855
	Testing	1.29	1.591	-0.494
	Complete	0.603	0.883	0.672

Note: WM1 - Wang-Mendel fuzzy algorithm model with nitrate and orthophosphate predictors; WM2 - Wang-Mendel fuzzy algorithm model with all water quality parameters predictors; WM 3 - Wang-Mendel fuzzy algorithm model with pH and dissolved oxygen predictors; MAE - Mean Absolute Error; RMSE - Root Mean Square Error; R - correlation coefficient.

Comparison of the WM2 and MLR depicted in scatter plots (Figure 3) revealed that the WM2 model performed better than the latter model. This is indicated by the coefficient of correlation of WM2, which was double the value of the correlation coefficient of the MLR model. The WM2 model produced predicted values that had a strong correlation with the observed data. Hence, the results of this study recognized that the suggested WM models are effective in estimating predictions of the freshwater phytoplankton biomass by utilizing all possible other water quality parameters.

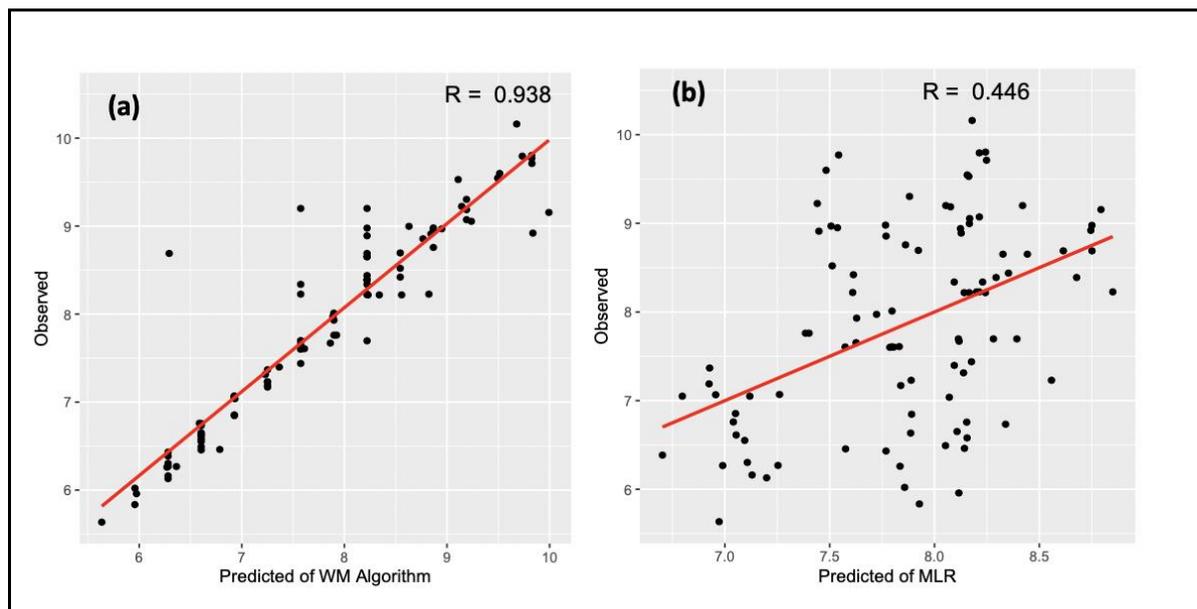


Figure 3. Scatter plot of observed and predicted biomass of freshwater phytoplankton; a - Wang-Mendel fuzzy algorithm model with all water quality parameters predictors model (WM2); b - multi linear regression (MLR) model.

**Conclusions.** The estimation of freshwater phytoplankton biomass is essential to prevent water eutrophication that may harm the aquatic ecosystem. Eutrophication is mainly caused by nutrient (nitrate and phosphate) enrichment. The results of this study indicated that WM models worked effectively in predicting freshwater phytoplankton biomass in East Java, Indonesia. It also showed that, rather than the eutrophication model (WM1), WM3 that included other water quality parameters was preferable. Moreover, this model also outperformed the MLR model that has been widely used as standard model for phytoplankton biomass.

## References

- Ahmed A. A. M., Shah S. M. A., 2017 Application of adaptive neuro-fuzzy inference system (ANFIS) to estimate the biochemical oxygen demand (BOD) of Surma River Journal of King Saud University - Engineering Sciences 29(3):237-243.
- Al-Hashmi K., Al-Azri A., Claereboudt M. R., Piontkovski S., Amin S. M. N., 2013 Phytoplankton community structure of a mangrove habitat in the arid environment of Oman: The dominance of *Peridinium quinquecorne*. Journal of Fisheries and Aquatic Science 8(5):595-606.
- Alvarez-Estevéz D., Moret-Bonillo V., 2018 Revisiting the Wang–Mendel algorithm for fuzzy classification. Expert Systems 35(4):e12268, 15 p.
- Amoatey P., Baawain M. S., 2019 Effects of pollution on freshwater aquatic organisms. Water Environment Research 91(10):1272-1287.
- Arend K. K., Beletsky D., DePinto J. V., Ludsins S. A., Roberts J. J., Rucinski D. K., Scavia D., Schwab D. J., Höök T. O., 2011 Seasonal and interannual effects of hypoxia on fish habitat quality in central Lake Erie. Freshwater Biology 56(2):366-383.
- Baban S. M. J., 1996 Trophic classification and ecosystem checking of lakes using remotely sensed information. Hydrological Sciences Journal 41(6):939-957.
- Barraza-Guardado R. H., Arreola-Lizárraga J. A., López-Torres M. A., Casillas-Hernández R., Miranda-Baeza A., Magallón-Barrajas F., Ibarra-Gómez C., 2013 Effluents of shrimp farms and its influence on the coastal ecosystems of Bahía de Kino, Mexico. The Scientific World Journal 2013:306370, 8 p.
- Bode A., Estévez M. G., Varela M., Vilar J. A., 2015 Annual trend patterns of phytoplankton species abundance belie homogeneous taxonomical group responses

- to climate in the NE Atlantic upwelling. *Marine Environmental Research* 110:81-91.
- Davidson K., Gowen R. J., Harrison P. J., Fleming L. E., Hoagland P., Moschonas G., 2014 Anthropogenic nutrients and harmful algae in coastal waters. *Journal of Environmental Management* 146:206-216.
- Gasparovica M., Novoselova N., Aleksejeva L., 2010 Using fuzzy logic to solve bioinformatics tasks. *Scientific Journal of Riga Technical University Computer Sciences* 42(1):99-105.
- Glibert P. M., Allen J. I., Bouwman A. F., Brown C. W., Flynn K. J., Lewitus A. J., Madden C. J., 2010 Modeling of HABs and eutrophication: Status, advances, challenges. *Journal of Marine System* 83(3):262-275.
- Gobler C. J., 2020 Climate change and harmful algal blooms: Insights and perspective. *Harmful Algae* 91:101731, 4 p.
- Gokulachandran J., Mohandas K., 2012 Application of regression and fuzzy logic method for prediction of tool life. *Procedia Engineering* 38:3900-3912.
- Hallegraeff G. M., 2010 Ocean climate change, phytoplankton community responses, and harmful algal blooms: A formidable predictive challenge. *Journal of Phycology* 46(2):220-235.
- Hazra A., Gogtay N., 2016 Biostatistics series module 6: Correlation and linear regression. *Indian Journal of Dermatology* 61(6):593-601.
- Herbeck L. S., Unger D., Wu Y., Jennerjahn T. C., 2013 Effluent, nutrient and organic matter export from shrimp and fish ponds causing eutrophication in coastal and back-reef waters of NE Hainan, tropical China. *Continental Shelf Research* 57:92-104.
- Inyang A. I., Wang Y. S., 2020 Phytoplankton diversity and community responses to physicochemical variables in mangrove zones of Guangzhou Province, China. *Ecotoxicology* 29:650-668.
- Kadim M. K., Arsad S., 2016 Distribution and density of microalgae based on coastal characteristic and ecology in Bone Bolango coastal region. *Asian Journal of Microbiology, Biotechnology and Environmental Sciences* 18(2):395-401.
- Kim T. H., Choi S. I., Lee W. J., 1999 Effects of acidification of stream water on freshwater algae 1. *Spirogyra*. *Algae* 14(2):127-132.
- Kozak A., Goldyn R., Dondajewska R., 2015 Phytoplankton composition and abundance in restored Maltański reservoir under the influence of physico-chemical variables and zooplankton grazing pressure. *PLoS ONE* 10(4):e0124738, 22 p.
- Lusiana E. D., Arsad S., Kusriani, Buwono N. R., Putri I. R., 2019a Performance of Bayesian quantile regression and its application to eutrophication modelling in Sutami Reservoir, East Java, Indonesia. *Ecological Questions* 30(2):69-77.
- Lusiana E. D., Arsad S., Kusriani, Buwono N. R., Putri I. R., 2019b The application of Bayesian quantile regression to analyse the relationship between nutrients content and phytoplankton abundance in Sutami reservoir. *IOP Conference Series: Earth and Environmental Science* 230:012082, 6 p.
- Lusiana E. D., Musa M., Mahmudi M., Buwono N. R., Utami K. P., 2020 Relationship analysis of N/P ratio and phytoplankton abundance in Ranu Pakis using regression approach. *IOP Conference Series: Earth and Environmental Science* 493:012021, 6 p.
- Lv J., Wu H., Chen M., 2011 Effects of nitrogen and phosphorus on phytoplankton composition and biomass in 15 subtropical, urban shallow lakes in Wuhan, China. *Limnologia* 41(1):48-56.
- Mahmudi M., Lusiana E. D., Arsad S., Buwono N. R., Darmawan A., Nisya T. W., Gurinda G. A., 2019 A study on phosphorus-based carrying capacity and trophic status index of floating net cages area in Ranu Grati, Indonesia. *AAFL Bioflux* 12(5):1902-1908.
- Manalu E. E., 2019 [Distribution of primary productivity in Selorejo reservoir, East Java]. Brawijaya University, 86 p. [In Indonesian].
- Mardiastuti F. W., 2019 [Analysis of water productivity using Trophic State Index (TSI) in Wlingi Raya reservoir, Blitar regency, East Java]. Brawijaya University, 103 p. [In Indonesian].

- Mulyanto M. R., 2019 [Water quality analysis using saprobic coefficient of phytoplankton community structure in Sengguruh reservoir]. Brawijaya University, 89 p. [In Indonesian].
- Musa M., Buwono N. R., Iman M. N., Ayuning S. W., Lusiana E. D., 2019 Pesticides in Kalisat river: Water and sediment assessment. *AAFL Bioflux* 12(5):1806-1813.
- Niu L., van Gelder P. H. A. J. M., Zhang C., Guan Y., Vrijling J. K., 2015 Statistical analysis of phytoplankton biomass in coastal waters: Case study of the Wadden Sea near Lauwersoog (The Netherlands) from 2000 to 2009. *Ecological Informatics* 30:12-19.
- Pasztaleniec A., 2016 Phytoplankton in the ecological status assessment of European lakes – advantages and constraints. *Environmental Protection and Natural Resources* 27(1):26-36.
- Prashanth D. S., Mehta R. V. K., Sharma N., 2020 Classification of handwritten Devanagari number - An analysis of pattern recognition tool using neural network and CNN. *Procedia Computer Science* 167:2445-2457
- Putra B. V., 2017 [Relationship of nitrate and phosphate to phytoplankton abundance in Lahor reservoir, Malang regency, Indonesia]. Brawijaya University, 112 p. [In Indonesian].
- Renaud S., Thinh L. V., Lambrinidis G., Parry D., 2002 Effect of temperature on growth, chemical composition and fatty acid composition of tropical Australian microalgae grown in batch cultures. *Aquaculture* 211(1-4):195-214.
- Riza L. S., Herrera F., Bergmeir C., Ben M., 2015 frbs: fuzzy rule-based systems for classification. *Journal of Statistical Software* 65(6), 30 p.
- Roosmini D., Septiono M. A., Putri N. E., Shabrina H. M., Salami I. R. S., Ariesyady H. D., 2018. River water pollution condition in upper part of Brantas River and Bengawan Solo River. *IOP Conference Series: Earth and Environmental Science* 106:012059, 7 p.
- Sari L. C., 2020 [Estimation of trophic status at Tanjungan reservoir using the chlorophyll-a method]. Brawijaya University, 98 p. [In Indonesian].
- Schober P., Schwarte L. A., 2018 Correlation coefficients: Appropriate use and interpretation. *Anesthesia and Analgesia* 126(5):1763-1768.
- Setyaningrum D., Agustina L., 2020 [Water quality analysis in Bengan Solo river watershed at Bojonegoro regency]. *Samakia Jurnal Ilmu Perikanan* 11(1):1-9. [In Indonesian].
- Søndergaard M., Larsen S. E., Jørgensen T. B., Jeppesen E., 2011 Using chlorophyll a and cyanobacteria in the ecological classification of lakes. *Ecological Indicators* 11(5):1403-1412.
- Sugiura N., Utsumi M., Wei B., Iwami N., Okano K., Kawauchi Y., Maekawa T., 2004 Assessment for the complicated occurrence of nuisance odours from phytoplankton and environmental factors in a eutrophic lake. *Lake and Reservoirs: Research and Management* 9(3-4):195-201.
- Takarina N. D., Patria M. P., 2017 Content of polyphenol compound in mangrove and macroalga extracts. *AIP Conference Proceedings* 1862:30100, 4 p.
- Tundo T., Sela E. I., 2018 Application of the fuzzy inference system method to predict the number of weaving fabric production. *International Journal on Informatics for Development* 7(1):20-28.
- Vrede T., Ballantyne A., Mille-Lindblom C., Algsten G., Gudasz C., Lindahl S., Brunberg A. K., 2009 Effects of N : P loading ratios on phytoplankton community composition, primary production and N fixation in a eutrophic lake. *Freshwater Biology* 54(2):331-344.
- Wang L. X., 2017 Modeling stock price dynamics with fuzzy opinion networks. *IEEE Transactions on Fuzzy Systems* 25(2):277-301.
- Wisha U. J., Ondara K., Ilham I., 2018 The influence of nutrient (N and P) enrichment and ratios on phytoplankton abundance in Keunekai waters, Weh Island, Indonesia. *Makara Journal of Science* 22(4):187-197.
- Xu Y., Schroth A. W., Isles P. D. F., Rizzo D. M., 2015 Quantile regression improves models of lake eutrophication with implications for ecosystem-specific management.

- Freshwater Biology 60(9):1841-1853.
- Yang X., Wu X., Hao H., He Z., 2008 Mechanisms and assessment of water eutrophication. *Journal of Zhejiang University Science B* 9(3):197-209.
- Yuan L. L., Pollard A. I., 2018 Changes in the relationship between zooplankton and phytoplankton biomasses across a eutrophication gradient. *Limnology and Oceanography* 63(6):2493-2507.
- \*\*\*APHA (American Public Health Association), 1989 Standard methods for the examination of water and wastewater. American Public Health Association, Washington DC, 874 p.

Received: 14 July 2020. Accepted: 11 September 2020. Published online: 07 January 2021.

Authors:

Evellin Dewi Lusiana, Faculty of Fisheries and Marine Science, Brawijaya University, 65145 Malang, Indonesia; AquaRES Research Group, Brawijaya University, 65145 Malang, Indonesia, e-mail: evellinlusiana@ub.ac.id  
Nanik Retno Buwono, Faculty of Fisheries and Marine Science, Brawijaya University, 65145 Malang, Indonesia; AquaRES Research Group, Brawijaya University, 65145 Malang, Indonesia, e-mail: buwonoretno@ub.ac.id

This is an open-access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution and reproduction in any medium, provided the original author and source are credited.

How to cite this article:

Lusiana E. D., Buwono N. R., 2021 Application of Wang-Mendel fuzzy algorithm to predict freshwater phytoplankton biomass in East Java, Indonesia. *AAFL Bioflux* 14(1):37-45.